

Activité 1

$$(n^2-n+2) \cdot a(n) - (n+2) \cdot (n+1) \cdot a(n+2) + 3 \cdot (n+1) \cdot a(n+1) = 0 \mid a(n+2) = w$$

$$-(n+1) \cdot (n+2) \cdot w + 3 \cdot a(n+1) \cdot (n+1) + a(n) \cdot (n^2-n+2) = 0$$

$$\text{solve}(-(n+1) \cdot (n+2) \cdot w + 3 \cdot a(n+1) \cdot (n+1) + a(n) \cdot (n^2-n+2) = 0, w)$$

$$w = \frac{3 \cdot a(n+1) \cdot (n+1) + a(n) \cdot (n^2-n+2)}{(n+1) \cdot (n+2)}$$

$$a(n+2) = \frac{3 \cdot a(n+1) \cdot (n+1) + a(n) \cdot (n^2-n+2)}{(n+1) \cdot (n+2)}$$

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$$a(n+2) = \frac{3 \cdot a(n+1) \cdot (n+1) + a(n) \cdot (n^2-n+2)}{(n+1) \cdot (n+2)} \mid_{n=m-2}$$

$$a(m) = \frac{3 \cdot a(m-1) \cdot (m-1) + a(m-2) \cdot (m^2-5 \cdot m+8)}{m \cdot (m-1)}$$

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©seqGen (la récursion a(n), l'indice n, le nom de la variable a, {n de départ, n final }, {a(0),a(1)}, l'incrément de n)

$$\text{seqGen} \left(\frac{3 \cdot a(n-1) \cdot (n-1) + a(n-2) \cdot (n^2-5 \cdot n+8)}{n \cdot (n-1)}, n, a, \{0,10\}, \{3,-2\}, 1 \right)$$

$$\left(3, -2, 0, \frac{-2}{3}, \frac{-1}{2}, \frac{-17}{30}, \frac{-31}{60}, \frac{-653}{1260}, \frac{-47}{96}, \frac{-43537}{90720}, \frac{-138947}{302400} \right)$$

$$c := \text{seqGen} \left(\frac{3 \cdot a(n-1) \cdot (n-1) + a(n-2) \cdot (n^2-5 \cdot n+8)}{n \cdot (n-1)}, n, a, \{0,10\}, \{3,-2\}, 1 \right)$$

$$\left(3, -2, 0, \frac{-2}{3}, \frac{-1}{2}, \frac{-17}{30}, \frac{-31}{60}, \frac{-653}{1260}, \frac{-47}{96}, \frac{-43537}{90720}, \frac{-138947}{302400} \right)$$

c[1]

3

$$\sum_{n=0}^6 (c[n+1] \cdot x^n)$$

$$\frac{-31 \cdot x^6}{60} - \frac{17 \cdot x^5}{30} - \frac{x^4}{2} - \frac{2 \cdot x^3}{3} - 2 \cdot x + 3$$

$$\text{sol}(x) := \frac{-31 \cdot x^6}{60} - \frac{17 \cdot x^5}{30} - \frac{x^4}{2} - \frac{2 \cdot x^3}{3} - 2 \cdot x + 3$$

Terminé

sol(0.5)

1.85964

Activité 2

$$c := \text{seqGen}\left(\frac{3 \cdot a(n-1) \cdot (n-1) + a(n-2) \cdot (n^2 - 5 \cdot n + 8)}{n \cdot (n-1)}, n, a, \{0, 50\}, \{3, -2\}, 1\right)$$

$$\left\{3, -2, 0, \frac{-2}{3}, \frac{-1}{2}, \frac{-17}{30}, \frac{-31}{60}, \frac{-653}{1260}, \frac{-47}{96}, \frac{-43537}{90720}, \frac{-138947}{302400}, \frac{-4472261}{9979200}, \frac{-54779}{126720}, \frac{-93741671}{222393600}, \frac{-60579863}{148262400}, \frac{-18627715387}{46702656000}, \frac{-10739397659}{27675648000}, \frac{-438087897493}{1154829312000}, \frac{-1025795453}{2771590348}\right\}$$

Terminé

$$\text{solu6}(x) := \sum_{n=0}^6 (c[n+1] \cdot x^n)$$

Terminé

$$\text{solu15}(x) := \sum_{n=0}^{15} (c[n+1] \cdot x^n)$$

Terminé

$$\text{solu30}(x) := \sum_{n=0}^{30} (c[n+1] \cdot x^n)$$

$$\text{solu6}(0.5) \qquad \qquad \qquad 1.85964$$

$$\text{solu15}(0.5) \qquad \qquad \qquad 1.85188$$

$$\text{solu30}(0.5) \qquad \qquad \qquad 1.85186$$

$$\text{solu15}(x)$$

$$\frac{-18627715387 \cdot x^{15}}{46702656000} - \frac{60579863 \cdot x^{14}}{148262400} + \frac{93741671 \cdot x^{13}}{222393600} - \frac{54779 \cdot x^{12}}{126720} + \frac{4472261 \cdot x^{11}}{9979200} - \frac{138947 \cdot x^{10}}{302400} + \frac{43537 \cdot x^9}{90720} - \frac{47 \cdot x^8}{96} + \frac{653 \cdot x^7}{1260} - \frac{31 \cdot x^6}{60} + \frac{17 \cdot x^5}{30} - \frac{x^4}{2} + \frac{2 \cdot x^3}{3}$$

